

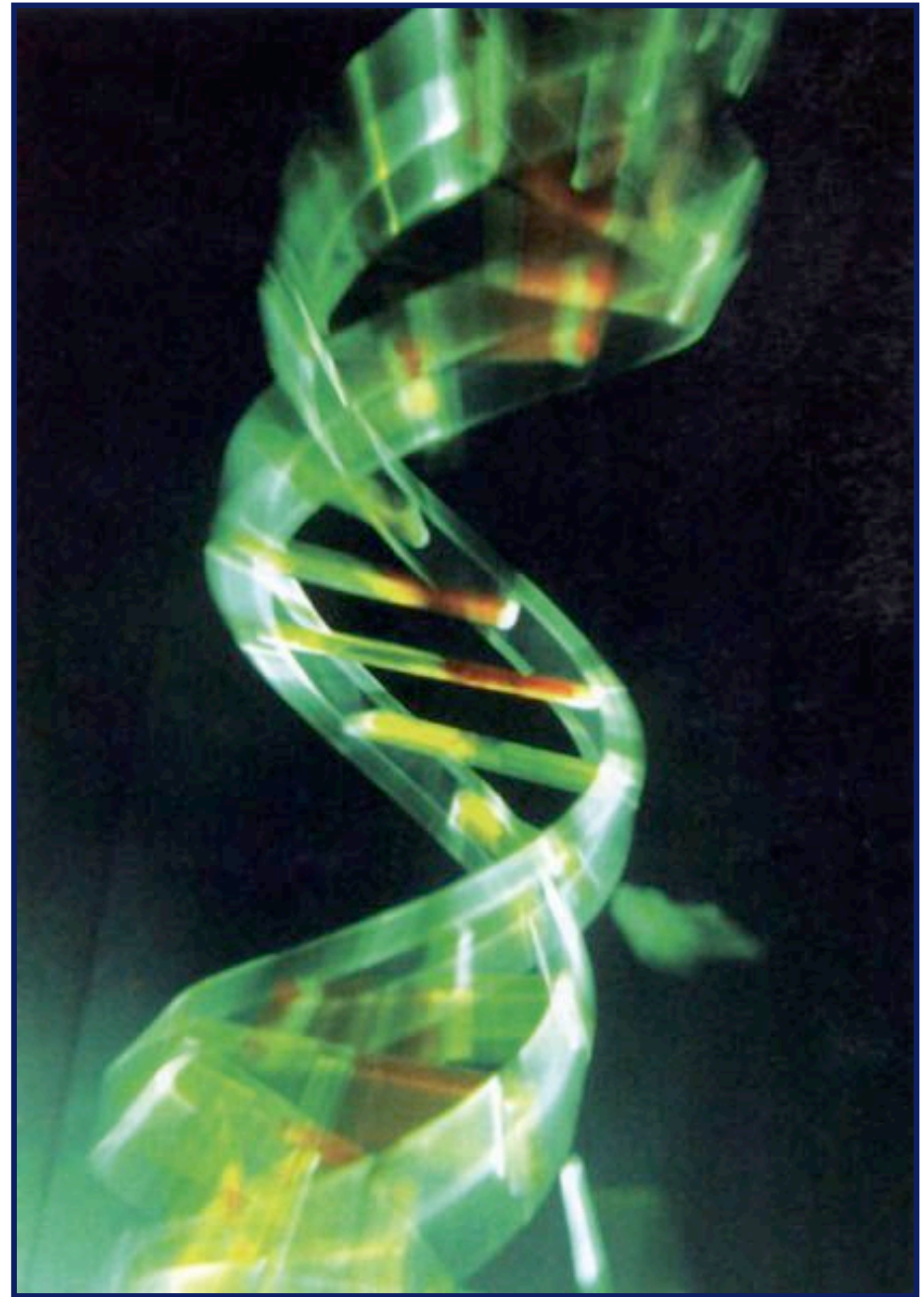
Chapter 6

Linkage Analysis and Mapping

Three point crosses

- mapping
- strategy
- examples

➤ Mapping human genes



Three point crosses

- Faster and more accurate way to map genes
- Simultaneous analysis of three markers
- Information on the position of three genes relative to each other can be obtained from one mating rather than two independent matings.
 - Example: *Drosophila* autosomal genes:
 - **vg** = vestigial wings; **vg+** = normal
 - **b** = black body; **b+** = normal body
 - **pr** = purple eyes; **pr+** = normal eyes
- Cross of pure breeding vestigial winged, black bodied, purple eyed female to a pure breeding wild type male:
 - **vgvg bb prpr** × **vg+vg+ b+b+ pr+pr+**

Three Factor Testcrosses Result in Eight Phenotypic Progeny Classes

P ♀ $vg\ b\ pr / vg\ b\ pr$ × ♂ $vg^+\ b^+\ pr^+ / vg^+\ b^+\ pr^+$

F₁ (all identical) $vg\ b\ pr / vg^+\ b^+\ pr^+$

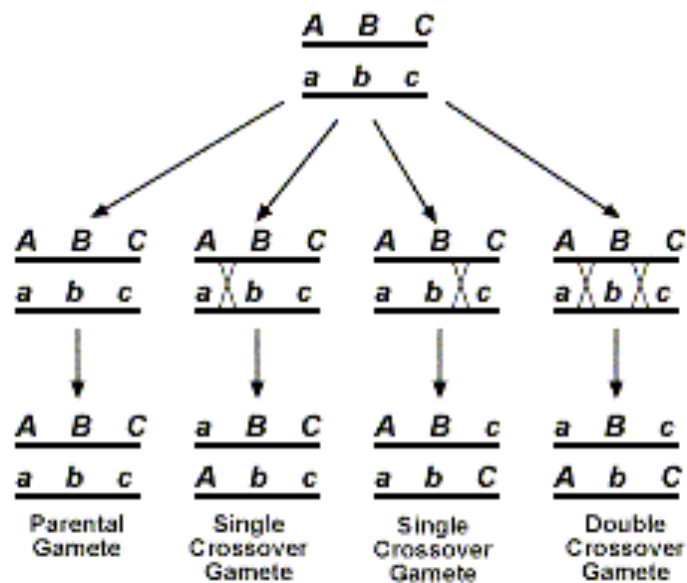
Test cross ♀ $vg\ b\ pr / vg^+\ b^+\ pr^+$ × ♂ $vg\ b\ pr / vg\ b\ pr$

Test cross progeny	1779	$vg\ b\ pr$	} Parental combinations for all three genes
	1654	$vg^+\ b^+\ pr^+$	
	252	$vg^+\ b\ pr$	} Recombinants for vg relative to parental combinations for b and pr
	241	$vg\ b^+\ pr^+$	
	131	$vg^+\ b\ pr^+$	} Recombinants for b relative to parental combinations for vg and pr
	118	$vg\ b^+\ pr$	
	13	$vg\ b\ pr^+$	} Recombinants for pr relative to parental combinations for vg and b
	9	$vg^+\ b^+\ pr$	

4197

Types of Gametes

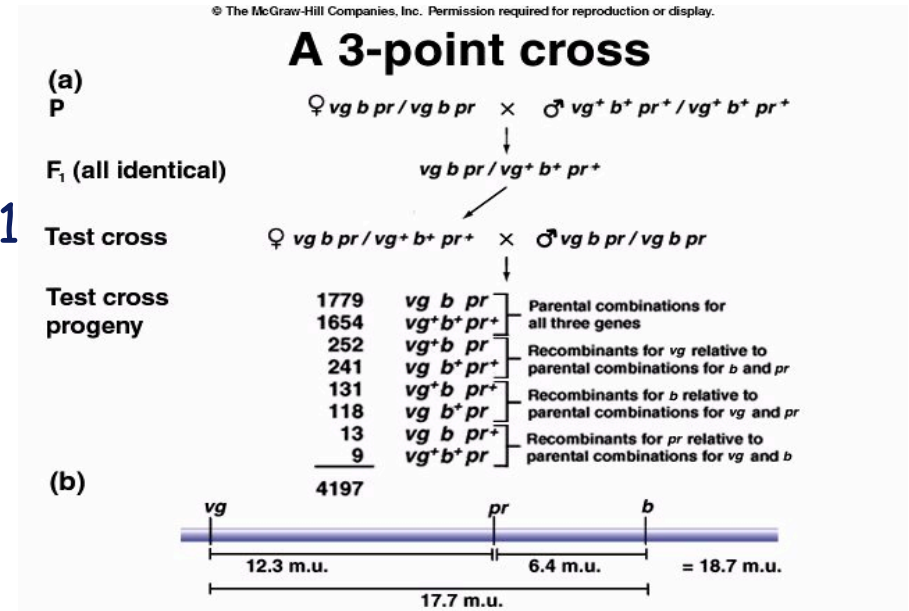
Parental and Recombinant Gametes
Derived from Three-Point Crosses



- Parental Types
- Single Crossover between A & B/a & b
- Single Crossover between B & C/b & C
- Double Crossover

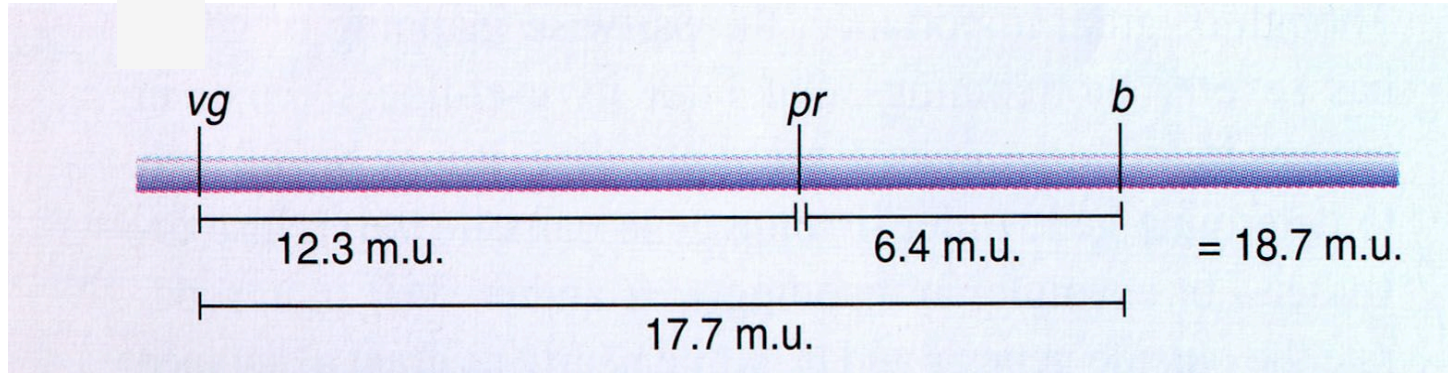
Data Analysis

- There are eight gametes from the F1
 - largest number is parental
 - smallest number is double crossover
- Identify the parental and recombinants
 - Two genes at a time.
 - Compare recombinant to parental
 - Double crossover change (oddball) is guy in the middle

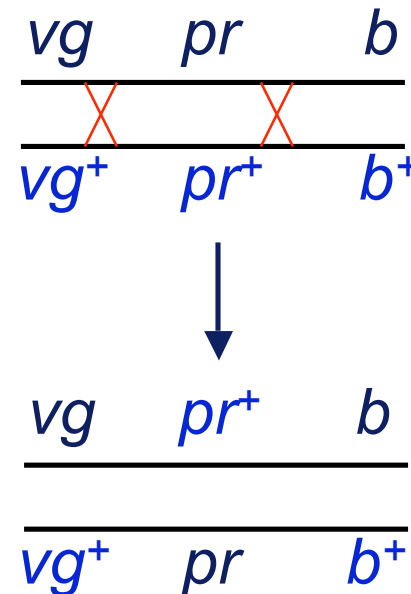


- Write order of genes
- The orientation from left to right is purely arbitrary.
- What the hell are you talking about??

Find the **double recombinant** class (the class with the least number of progeny) -- the gene that is different from the parental chromosome in this class is the middle gene.



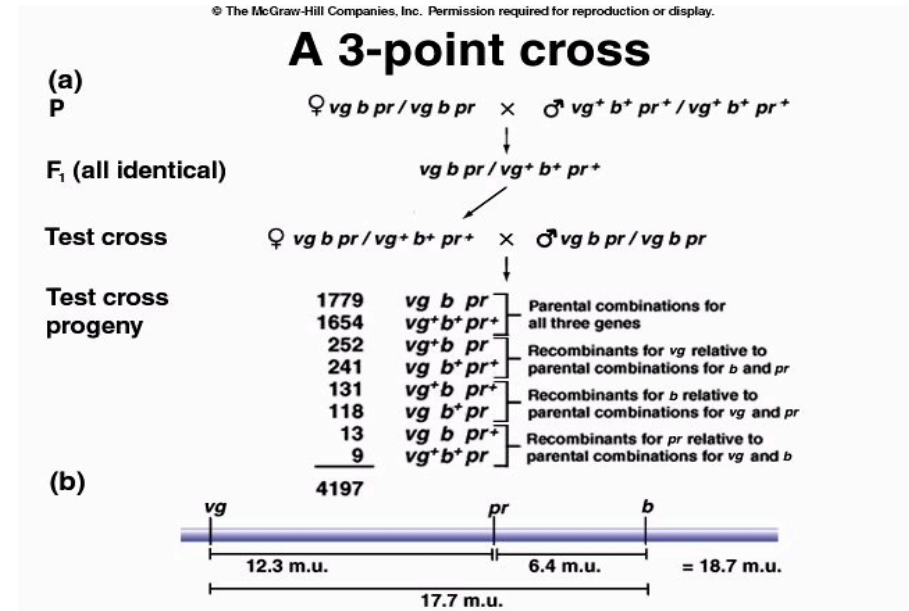
1779	<i>vg b pr</i>	} P
1654	<i>vg⁺ b⁺ pr⁺</i>	
252	<i>vg⁺ b pr</i>	
241	<i>vg b⁺ pr⁺</i>	
131	<i>vg⁺ b pr⁺</i>	
118	<i>vg b⁺ pr</i>	
13	<i>vg b pr⁺</i>	} DCO
9	<i>vg⁺ b⁺ pr</i>	



double
cross over
chromosomes

Data Analysis

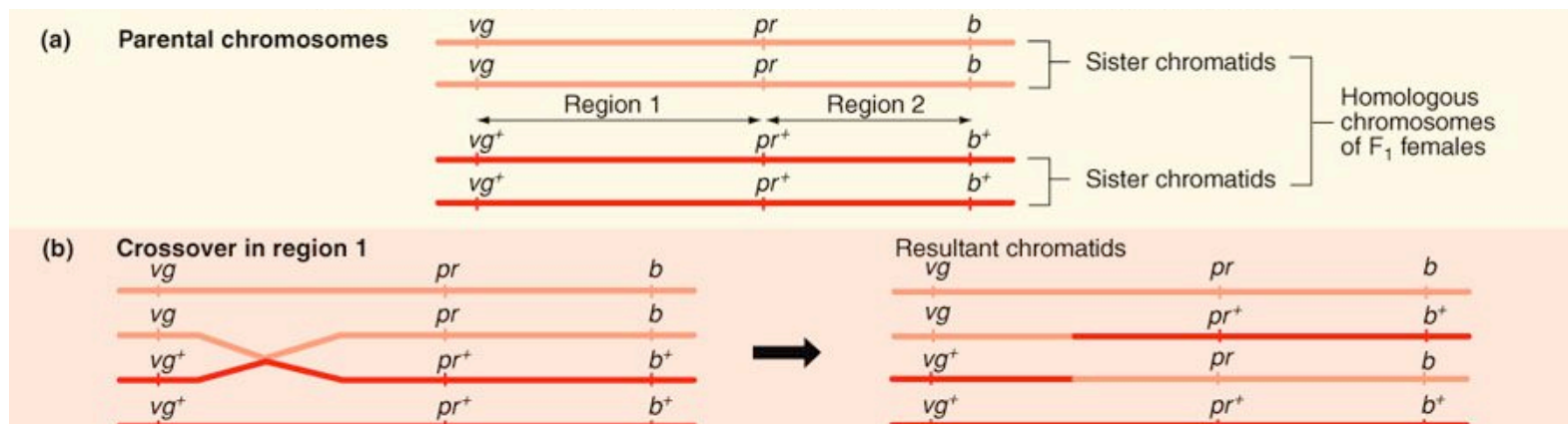
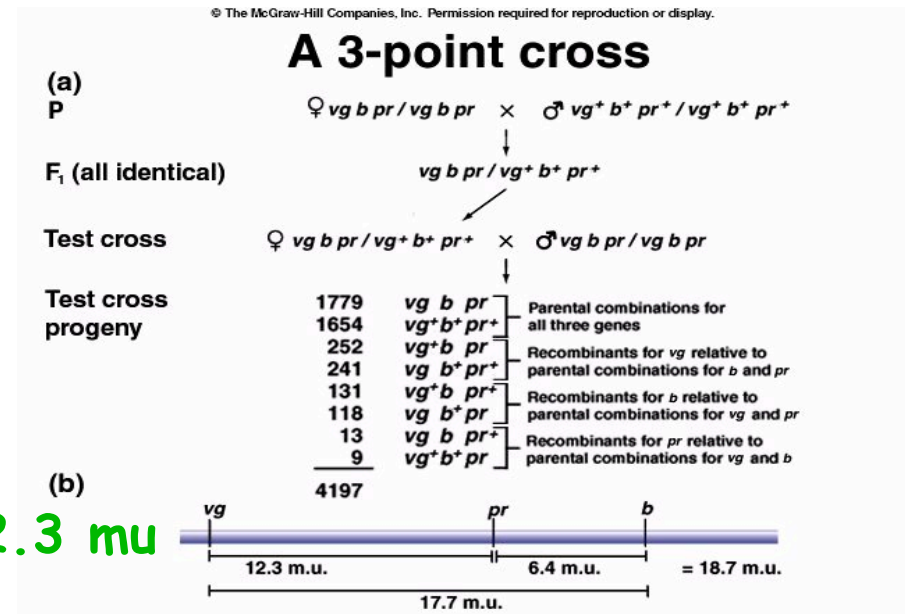
- There are eight gametes from the F1
 - largest number is parental (P)
 - smallest number is double crossover (DCO)
- Identify the parental and recombinants
 - Two genes at a time.
 - Compare recombinant to parental
 - Double crossover change (oddball) is guy in the middle
 - Compare DCO to P
 - 2 genes should be the same,
 - one should be the opposite. (the oddball)
 - Check both to check yourself
 - Write order of genes
- $vg - pr - b$
 - The orientation from left to right is purely arbitrary.
- Now determine which numbers go to which genes.
 - Find the numbers where the "vg" is the oddball and others are same
 - These are numbers for vg to pr region. (252 and 241)
- What the hell are you talking about????????????????????????????????????



Analyzing the results of a three point cross

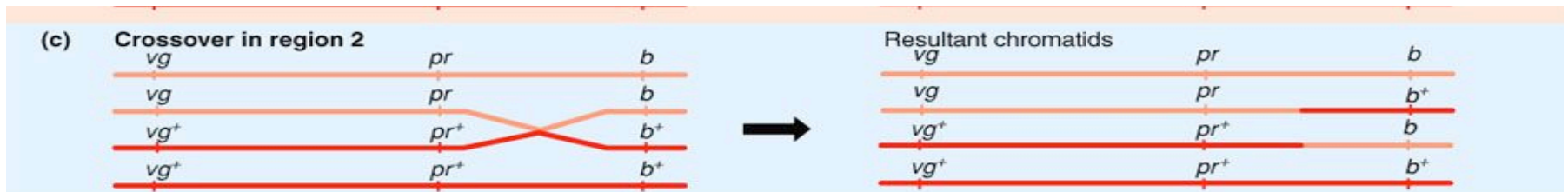
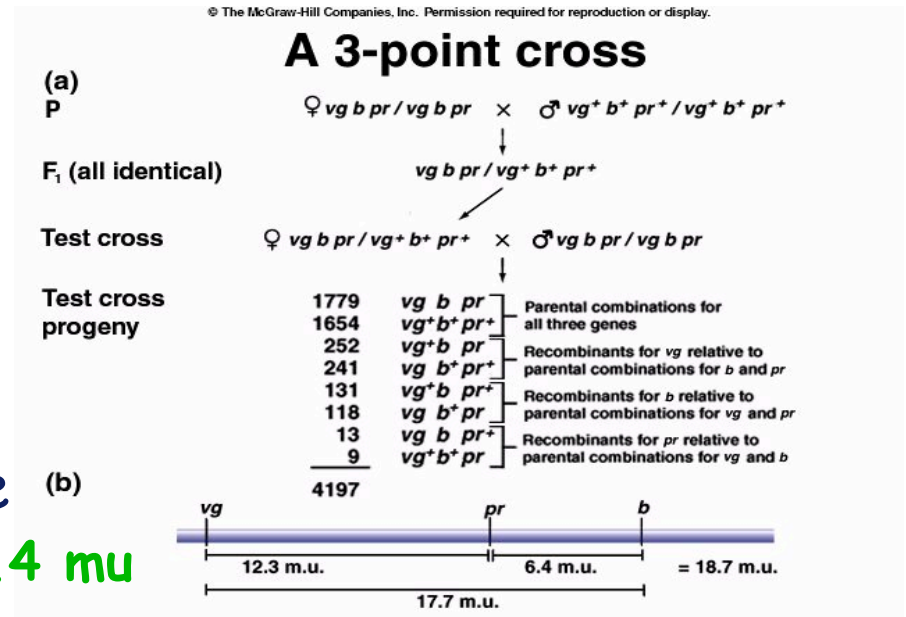
- Look at two genes at a time and compare to parental
 - *vg* and *pr*
- vg-pr* parentals are:
 - *vg - pr - b*
 - *vg+ - pr+ - b+*
- vg-pr* recombinants are:
 - *vg+ - pr - b*
 - *vg - pr+ - b*
- Numbers that correspond are

$$\frac{252+241+13+9}{4197} = 0.123 \times 100 = 12.3 \text{ mu}$$



Analyzing the results of a three point cross

- Look at two genes at a time
- and compare to parental
 - $Vg - pr - b$
 - $Vg^+ - pr^+ - b^+$
- b-pr recombinants are:
 - $Vg^+ - b - pr^+$
 - $Vg - b^+ - pr$
- Numbers that correspond are
 - $\frac{131+118+13+9}{4197} = 0.064 \times 100 = 6.4 \text{ mu}$



Analyzing the results of a three point cross

- Look at two genes at a time and compare to parental
 - *vg* and *b*

- *vg*-*b* recombinants are:

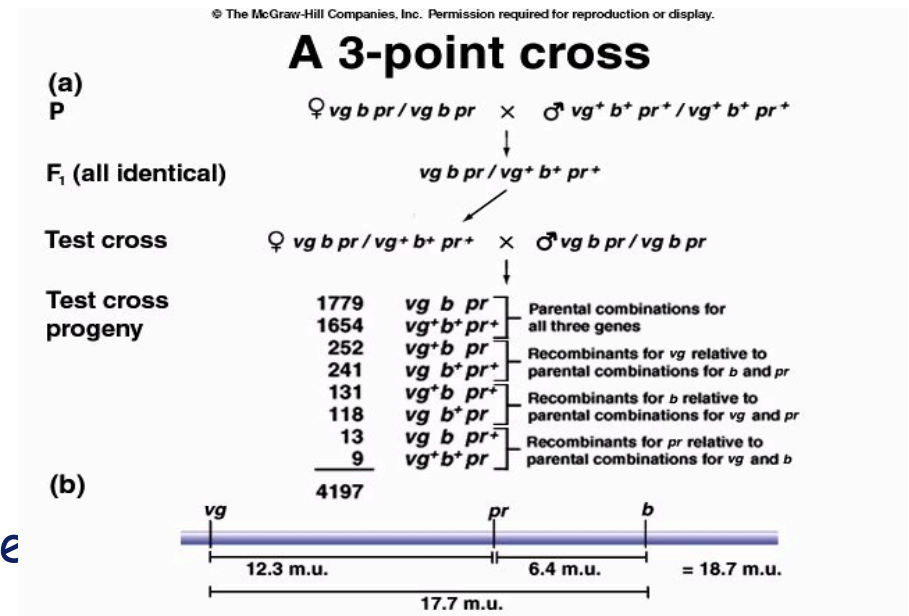
- *vg*-*b*⁺
- *vg*⁺-*b*

- This checks to be sure you have
 - the correct middle gene also.
 - Should be the largest distance

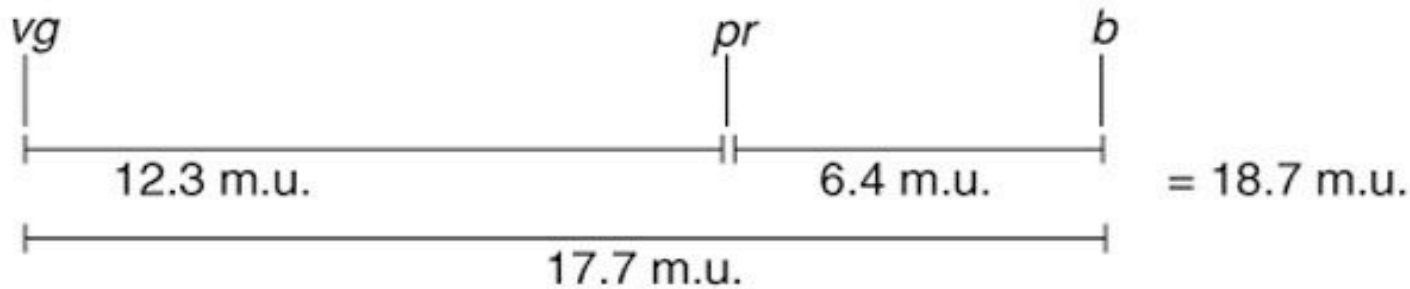
- Numbers that correspond are

$$\frac{252 + 241 + 131 + 118 + 13 + 13 + 9 + 9}{4197} \times 100 = 18.7 \text{ m.u.}$$

- Why count dco twice?



(b) Deduced genetic map



WRONG Without dco

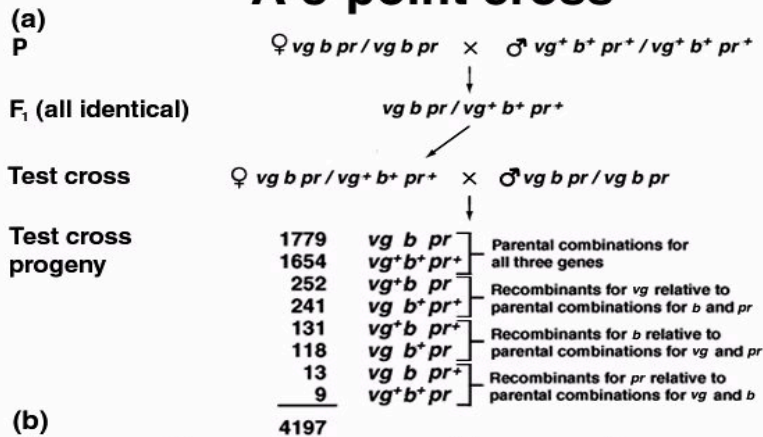
→ $vg - b$ dist $\frac{252 + 241 + 131 + 118}{4197} \times 100 = 17.7$ m.u.

$vg - pr$ dist $\frac{252 + 241 + 13 + 9}{4197} \times 100 = 12.3$ m.u.

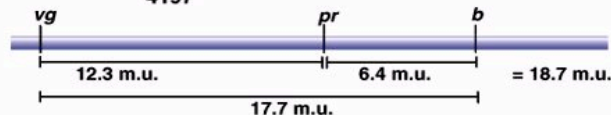
$b - pr$ dist $\frac{131 + 118 + 13 + 9}{4197} \times 100 = 6.4$ m.u.

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A 3-point cross



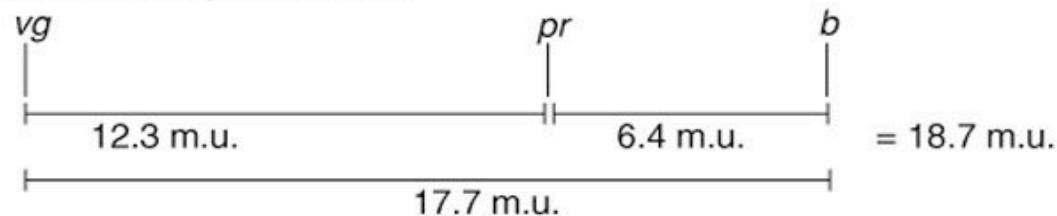
17.7 m.u. is not 18.7 m. u. !!!!!!!

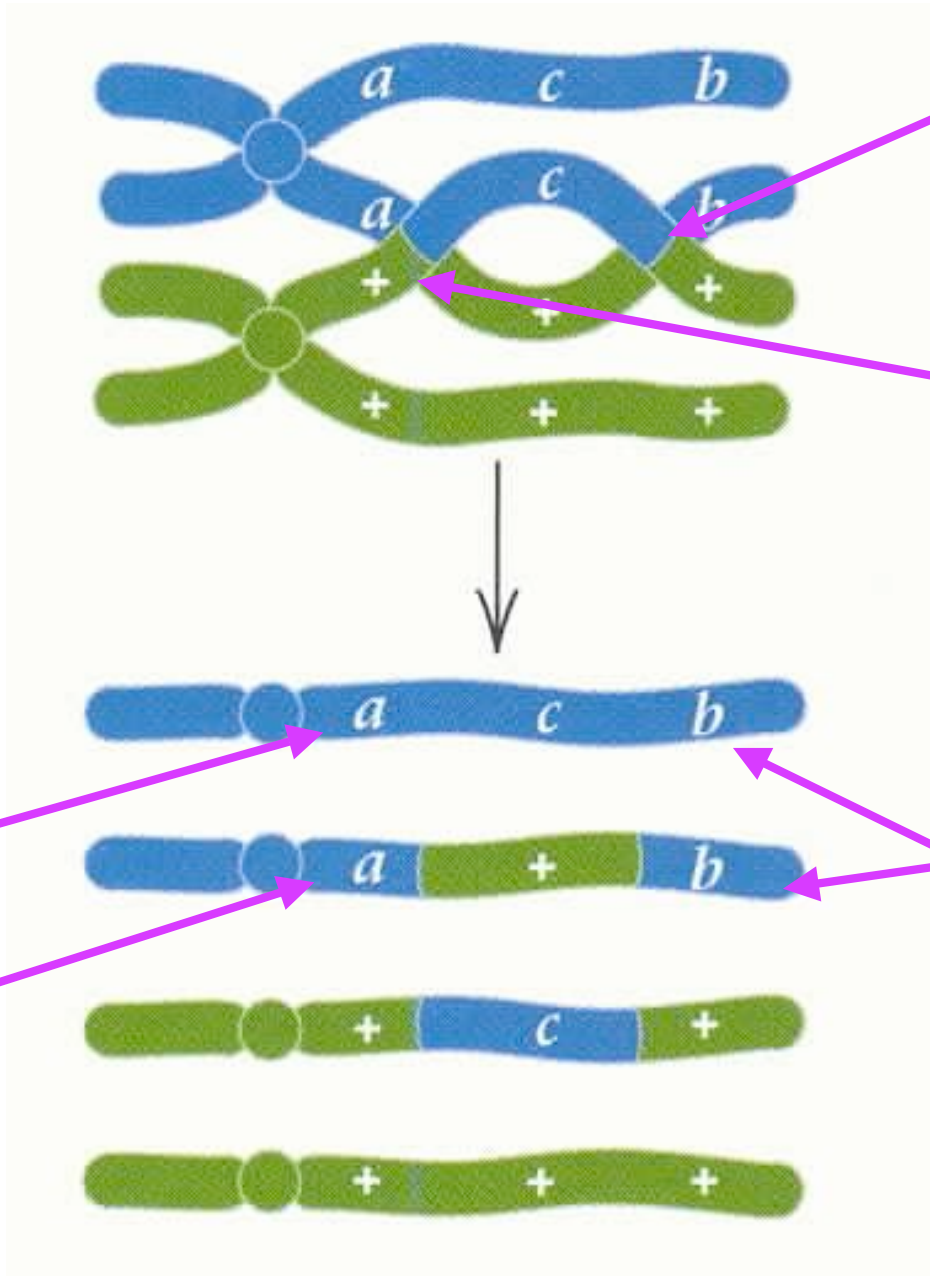


Double Crossovers

- Recombination is caused by formation of chiasmata along the chromosome at multiple points.
- If the distance between two genes is large enough, there can potentially be multiple chiasmata formation between them;
 - so there could be multiple crossovers.
- What would happen if there were two crossovers between the two outside genes (in this case *vg* and *b*)?
 - **Answer:** there would appear to be fewer recombinants between the two genes:
 - it would appear as if the genes are closer;
 - the calculated map distance between these genes will be less than actual.

(b) Deduced genetic map





Two recombination events occurred in the interval between a and b.

- We must count them for each of the single crossover events.

- They are crossing over events that occur on both sides.

- Must be used twice in calculations

➤ We need to add the number of double recombinants **TWICE** to our total for the outside markers:

1779	<i>vg</i>	<i>b</i>	<i>pr</i>	} P
1654	<i>vg⁺</i>	<i>b⁺</i>	<i>pr⁺</i>	
252	<i>vg⁺</i>	<i>b</i>	<i>pr</i>	
241	<i>vg</i>	<i>b⁺</i>	<i>pr⁺</i>	
131	<i>vg⁺</i>	<i>b</i>	<i>pr⁺</i>	
118	<i>vg</i>	<i>b⁺</i>	<i>pr</i>	
13	<i>vg</i>	<i>b</i>	<i>pr⁺</i>	} DCO
9	<i>vg⁺</i>	<i>b⁺</i>	<i>pr</i>	

vg-b distance...

$$\frac{252 + 241 + 131 + 118 + \mathbf{13 + 9 + 13 + 9}}{4197} \times 100 = \mathbf{18.7} \text{ m.u.}$$

Question

- Which type of class would you expect to account for the lowest frequency?
 - 1) Parental
 - 2) Single Recombinants
 - 3) Double Recombinants
 - 4) Middle class

Do Genetic and Physical maps correspond?

- Order of genes is correctly predicted by physical maps
- Distance between genes is **not** always similar to physical maps
 - Double, triple, and more crossovers
 - Only 50% recombination frequency observable in a cross
 - Variation across chromosome in rate of recombination
- Mapping functions compensate for inaccuracies, but are often imprecise.
- In addition, a process called Interference may occur.

Interference: The number of double crossovers may be less than expected

- Sometimes the number of observable double crossovers is less than expected if the two exchanges are not independent
 - Occurrence of one crossover reduces likelihood that another crossover will occur in adjacent parts of the chromosome
 - **Chromosomal interference** -
 - crossovers do not occur independently
 - Interference is not uniform among chromosomes or even within a chromosome

Interference

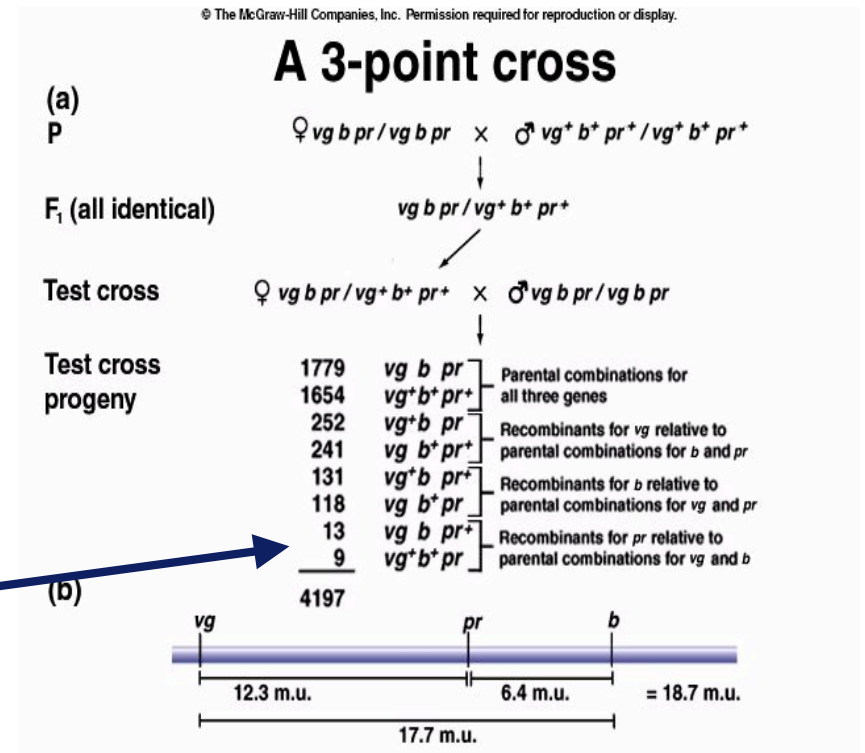
- The product rule allows us to predict the likelihood of a double crossover from the individual probabilities of each single crossover

$$\begin{array}{rcc}
 \text{Expected} & & \text{Probability} & & \text{Probability} \\
 \text{(double crossover)} & = & \text{(single crossover)} & \times & \text{(single crossover)} \\
 0.00787 & = & 0.064 & \times & 0.123
 \end{array}$$

- If we analyzed a total of
- 4197 fly offspring
 - The expected number
 - of double crossover offspring is

$$= 4197 \times 0.00787 = 33$$

- Observed number is 22



Interference

- Therefore, we would expect 33 offspring to be produced as a result of a double crossover
 - However, the observed number was only 22!
- This lower-than-expected value is due to a common genetic phenomenon, termed **interference**
 - The first crossover decreases the probability that a second crossover will occur nearby

Measuring interference

- Coefficient of coincidence =
 - ratio between actual or observed dco and expected dco
- coefficient of coincidence :
 - = observed dco / expected dco
- Interference = $1 - \text{coefficient of coincidence}$

$$p(\text{crossover in region 1}) \times p(\text{crossover in region 2}) =$$

$$.123 \times .064 = .0078$$

from a total of 4197 progeny, we should have seen (**expect**)
 $.0078 \times 4197 = 32.7$ or about 33 double recombinants

1779	<i>vg</i>	<i>b</i>	<i>pr</i>
1654	<i>vg+</i>	<i>b+</i>	<i>pr+</i>
252	<i>vg+</i>	<i>b</i>	<i>pr</i>
241	<i>vg</i>	<i>b+</i>	<i>pr+</i>
131	<i>vg+</i>	<i>b</i>	<i>pr+</i>
118	<i>vg</i>	<i>b+</i>	<i>pr</i>
13	<i>vg</i>	<i>b</i>	<i>pr+</i>
9	<i>vg+</i>	<i>b+</i>	<i>pr</i>
<hr/>			
4197			

$$I = 1 - C \text{ of } C$$

$$I = 1 - \frac{\text{Observed \# DCO}}{\text{Expected \# DCO}}$$

$$I = 1 - \frac{13 + 9}{33} = 0.333 \text{ or } 33.3\%$$

- This suggests that a cross over in one gene interval physically inhibited a crossover in adjacent regions by 33.3%.

Question

A plant heterozygous for three dominant traits N, T, and U is test crossed, the resulting progeny are as follows:

N	U	T	2
n	u	T	70
N	u	T	21
n	u	t	4
N	U	t	82
n	U	t	21
n	U	T	13
N	u	t	17

What is the linkage arrangement of the N, U and T alleles in the parental?

What is the linkage arrangement of the N, U and T alleles in the dco?

Which gene is in the middle?

- 1) N
- 2) U
- 3) T

Three Point Cross -- Example where order is not known: start with
2 pure breeding strains, F1 test crossed.

Testcross offspring

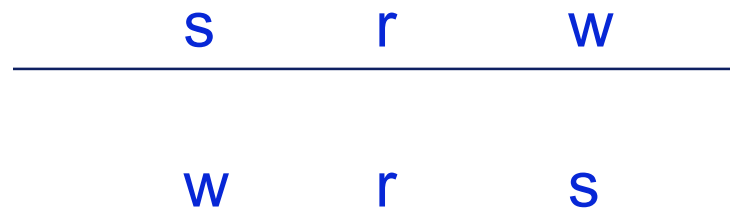
<u>progeny phenotype</u>	<u>number</u>
+++	6
r++	359
rs+	98
rsW	4
r+w	47
+s+	43
+sW	351
++w	92

Testcross offspring

<u>phenotype</u>	<u>number</u>
+++	6
r++	359
rs+	98
rsw	4
r+w	47
+s+	43
+sw	351
++w	92

largest class:	r++	359
	+sw	351
smallest class:	+++	6
	rsw	4

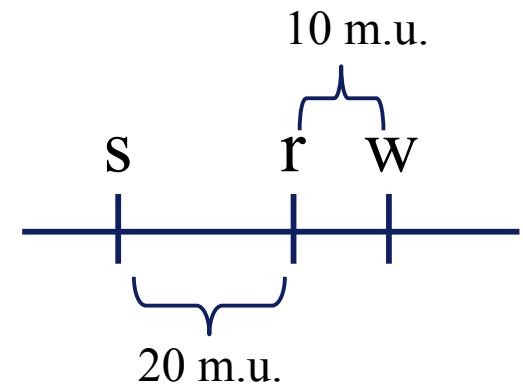
Order: determine an order where it takes two cross-overs to go from parentals to DCO.



The order of three markers is: s-r-w or w-r-s

- Next, sort according to reciprocal products and determine where crossovers occur:

<u>F2 products</u>	<u>#</u>	<u>class</u>
+ r +	359	parental
s + w	351	parental
s r +	98	SCO(s-r)
+ + w	92	SCO(s-r)
+ r w	47	SCO(r-w)
s + +	43	SCO(r-w)
+ + +	6	DCO
s r w	4	DCO

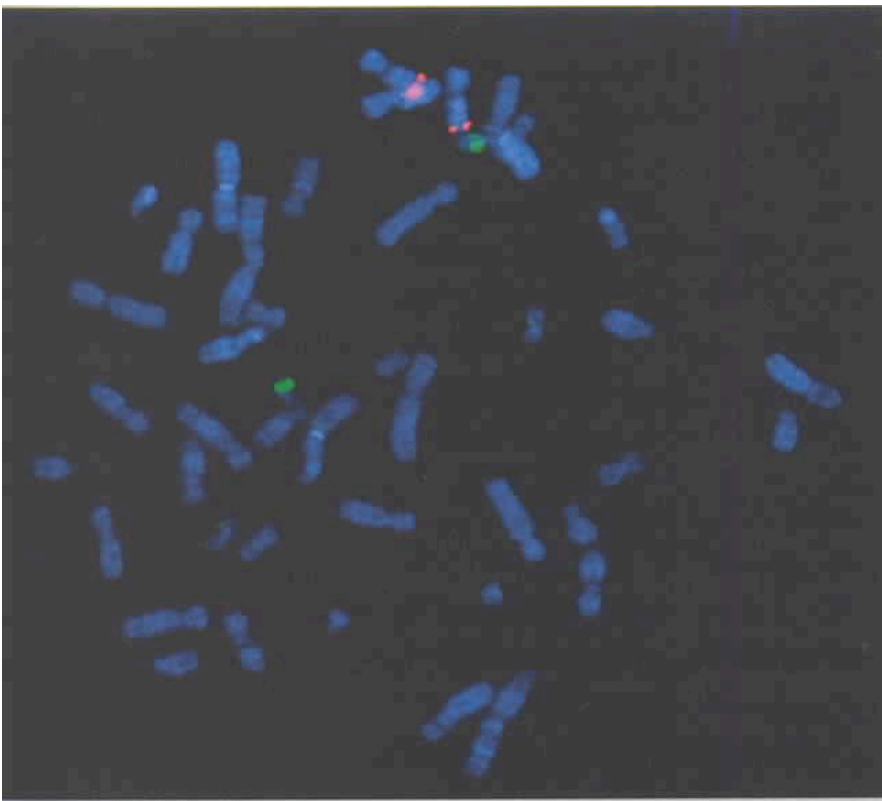


$$\text{map distance s-r} = \frac{98+92+6+4}{1000} = 0.20 = 20 \text{ m.u.}$$

$$\text{map distance r-w} = \frac{47+43+6+4}{1000} = 0.10 = 10 \text{ m.u.}$$

Recent Advances in the Field

Fluorescent *in situ* hybridization can also be used to localize cloned genes to a particular chromosome.



Probe for a specific gene



Visualized with chromosome specific probes

Homework Problems

Chapter 6

19, 20, 21, 22, 23, 24, 27

- DON'T forget to take the online QUIZ!!
- DON'T forget to submit the online iActivity
 - "Tomato"